# ON DESCRIPTION LOGICS

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#### DL's vs. First-Order Logic

- First-order logic (FOL) is very expressive, but is only semi-decidable
- DL's are a subset of FOL with limited expressiveness as a trade-off for decidability or more efficient decision problems
- Not all DL's are the same there are many varieties depending on which operators are allowed

## Expressiveness



## **DL** Operators

DL's are typically named by the operators they allow, showing their expressivity:

- AL: Attributive Language
- **C:** Complex Concept Negation
- S: ALC with Transitive Roles
- H: Role Hierarchy
- O: Nominals
- I: Inverse Properties
- N: Cardinality Restrictions
- (D): Use of Datatype Properties
- SHOIN<sup>(D)</sup> (OWL-DL is based on this) is a DL that allows all of these operators

## **DL** Operators

Some more operators:

- F: Functional Properties
- U: Concept Union
- E: Full Existential Qualification
- Q: Qualified Cardinality Restrictions
- SHOIN<sup>(D)</sup>, for example, is a DL without existential qualification (E), and therefore cannot express many things that can be expressed in FOL

 $\Box \exists x (Person(x) \land \forall y (Time(y) \rightarrow Hungry(x)))$ 

#### **Trade-Offs**

- □ Why use DL's?
  - Can be fully decidable, unlike FOL
  - Even when semi-decidable, can still have much more efficient decision problems
- What is lost from FOL?
  - Expressivity Every operator lost is expressivity lost
  - Completeness Can no longer derive every truth

#### Questions